

# Neutron Reflection Conditions for Magnetic Lattice and Symmetry Operations

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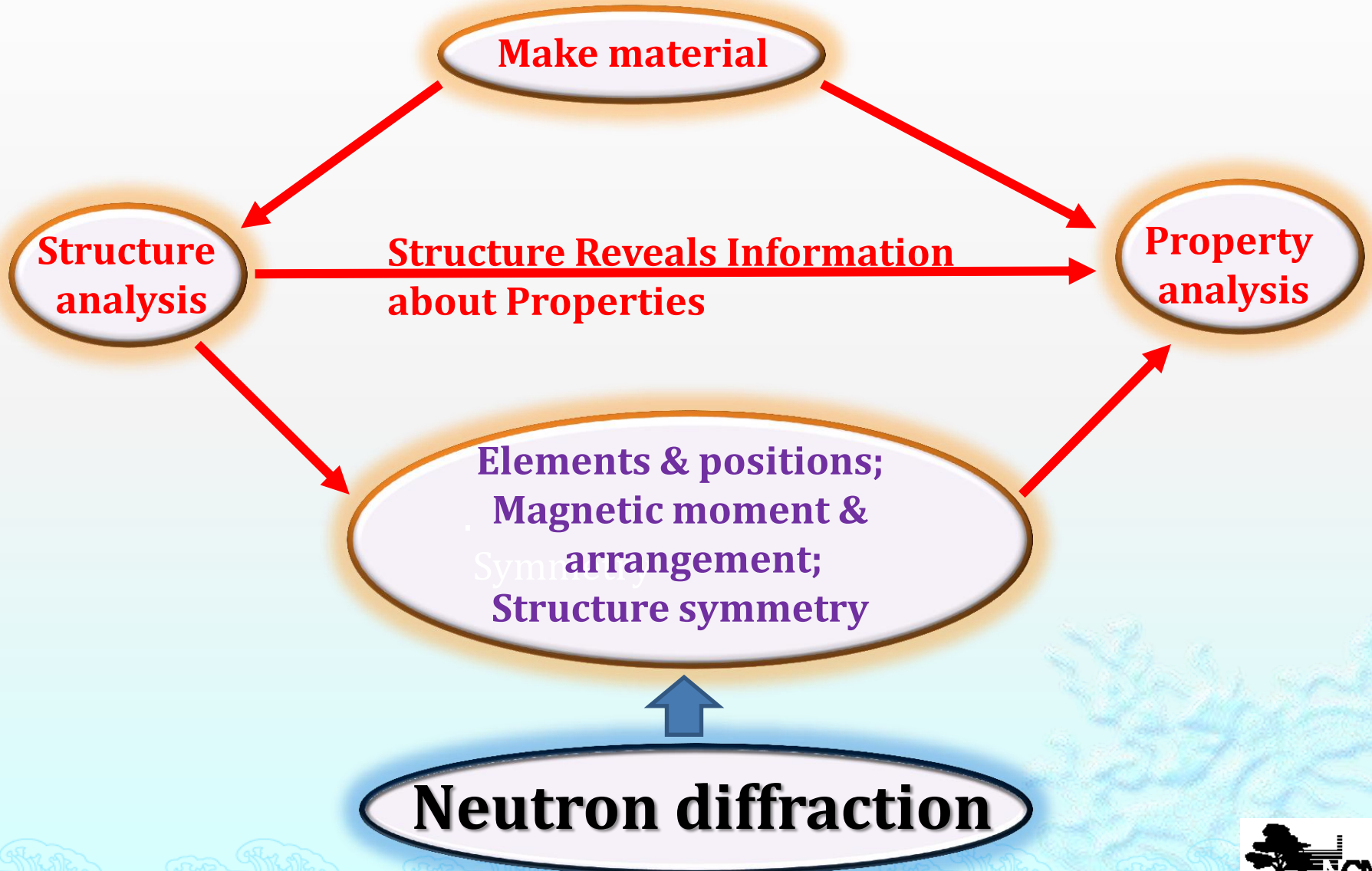
[www.ncnr.nist.gov](http://www.ncnr.nist.gov)

# Outline

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1. **Structure of materials science;**
2. **Black and white magnetic lattices and symmetry operations**
3. **Reflection condition analysis;**
4. **Reflection conditions for magnetic lattices;**
5. **Reflection conditions for magnetic symmetry operations;**
6. **Discussion.**

# Structure in materials science



# Structure determination from neutron powder diffraction for $K_{0.8}Fe_{1.6}Se_2$

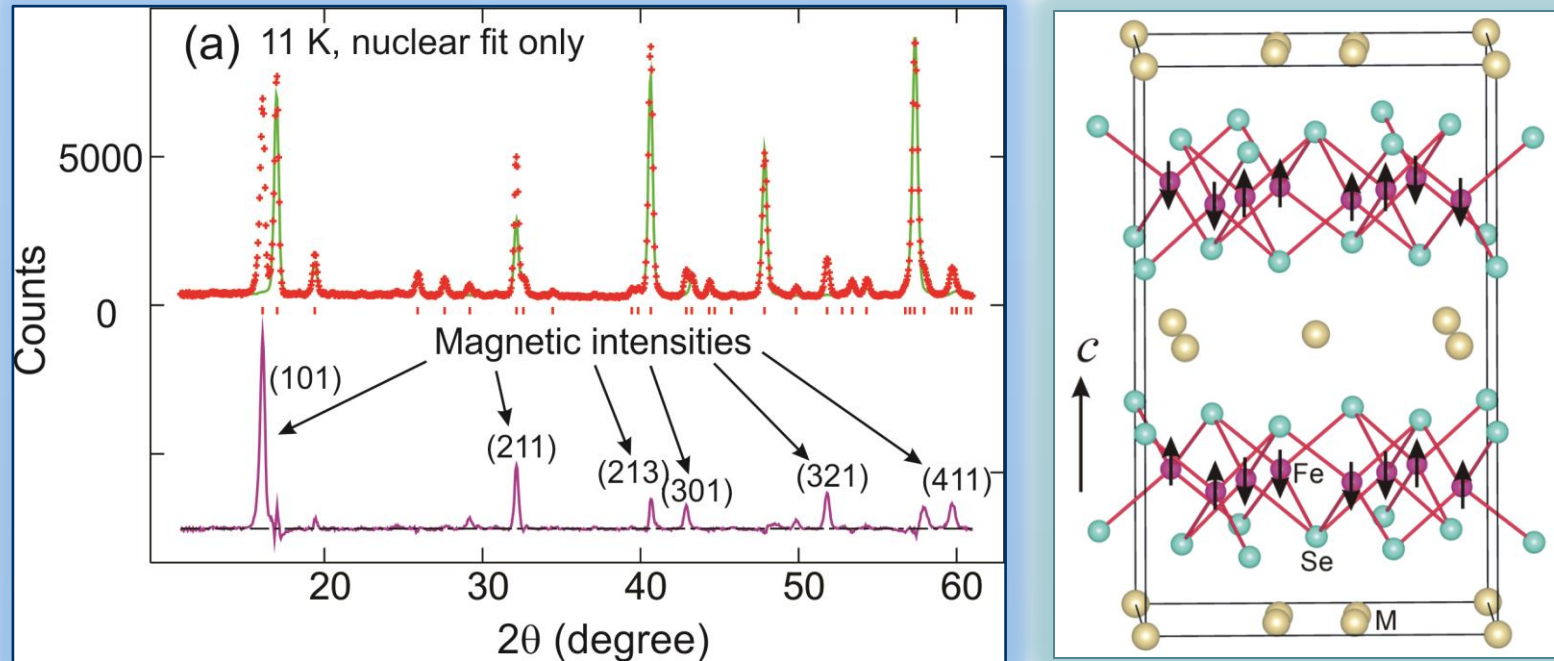


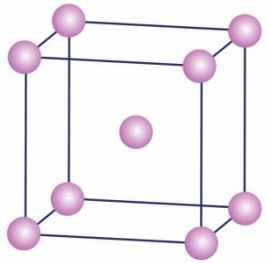
Fig. 1. (a) Neutron powder diffraction and (b) crystal and magnetic structures for  $K_xFe_{2-x}Se_2$  superconductor. In (a), we have:

- 1) Peak position:  $2d\sin\theta = n\lambda$ ;
- 2) Nuclear diffraction intensities:  $I_N = C\mathcal{M}_T^2 [(\gamma e^2)/(2mc^2)]^2 |F_N|^2$ ;
- 3) Magnetic diffraction intensities:  $I_M = C\mathcal{M}_T^2 A(\theta_B) [(\gamma e^2)/(2mc^2)]^2 <1 - (\tau \cdot M)^2> |F_M|^2$ .

**Magnetic reflection:  $h+k+l=2n$ , Body center?**

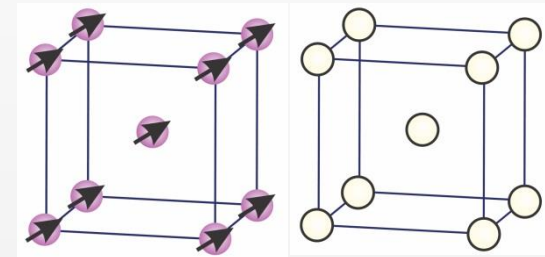
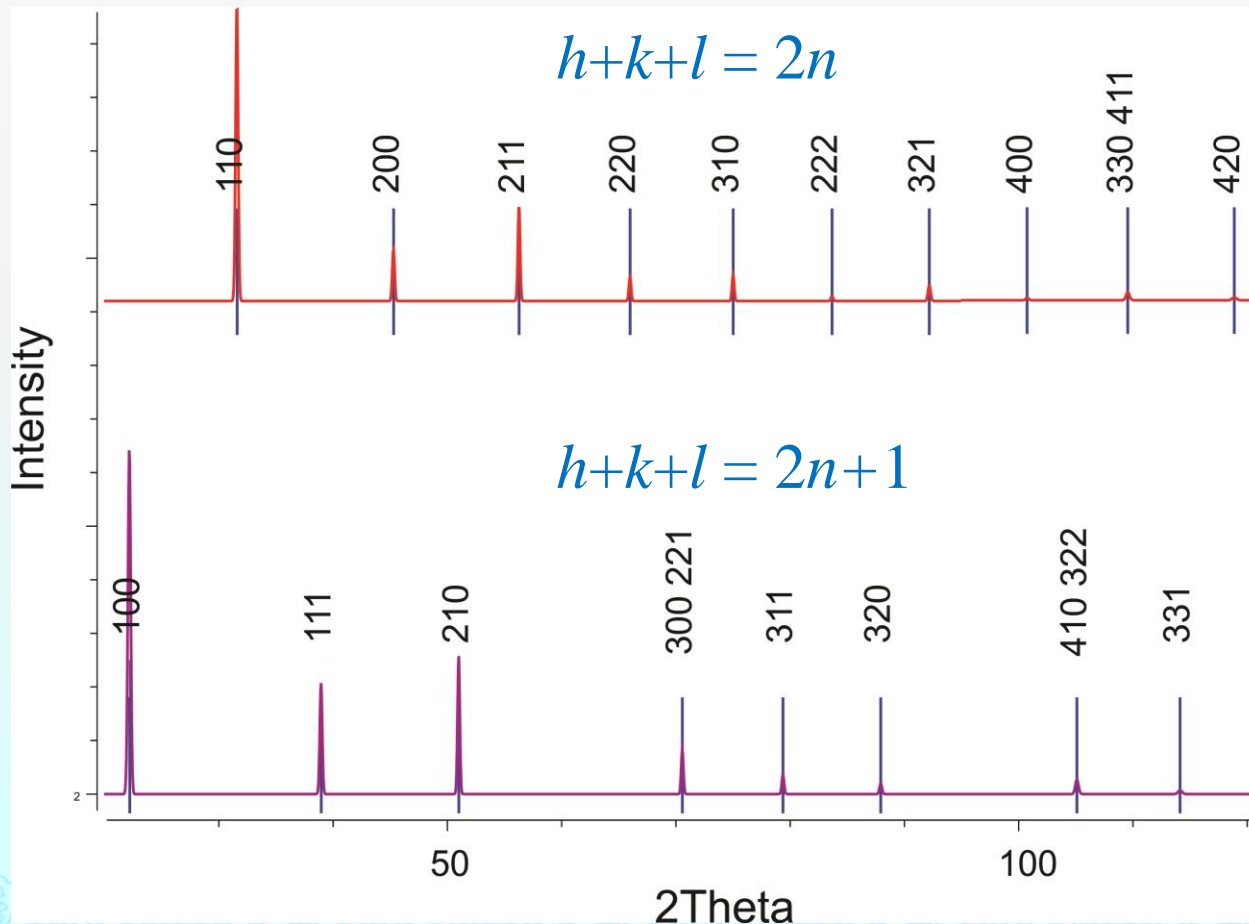
$$F_{hkl} = \sum p \exp(2\pi i(hx/a_0 + ky/b_0 + lz/c_0))$$

# Determine reflection conditions from magnetic structure factor $F_{hkl}$ calculations

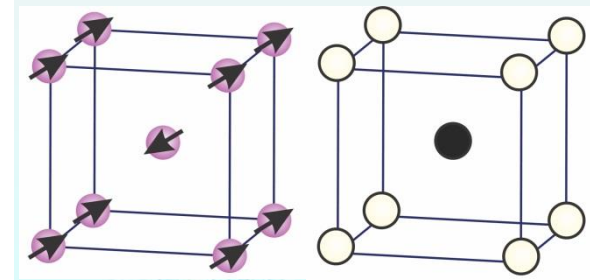


Nuclear  
For  $h k l$   
 $h+k+l = 2n$   
Is known

$$F_{hkl} = \sum \mathbf{p} \exp(2\pi i(\mathbf{h}x/a_0 + \mathbf{k}y/b_0 + \mathbf{l}z/c_0))$$



Ferromagnetic

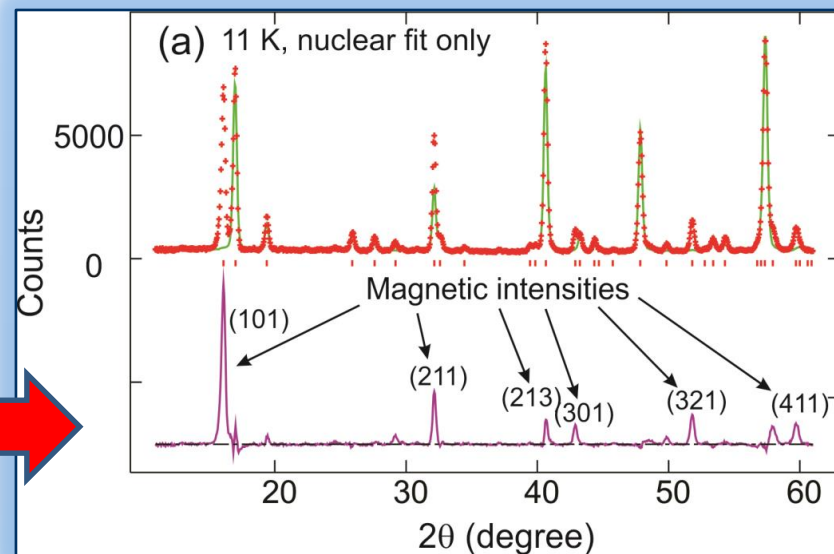


Antiferromagnetic



# Data collection and analysis

BT1 32-counter high-resolution  
neutron powder diffractometer at NCNR

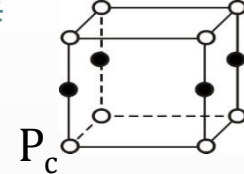
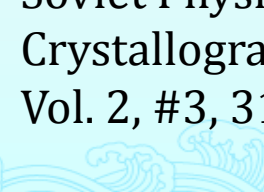
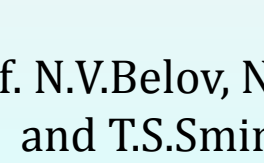
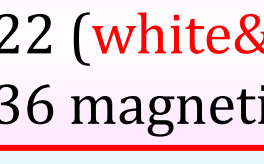
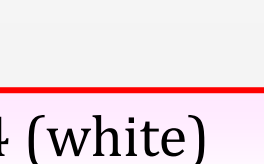
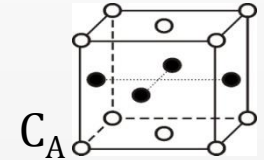
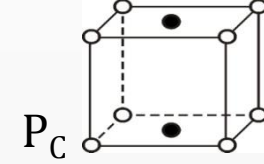
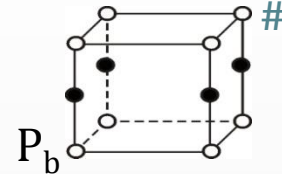
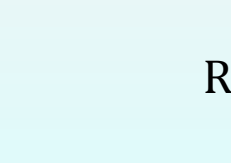
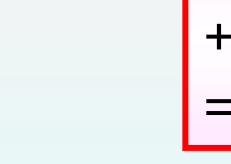
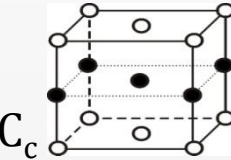
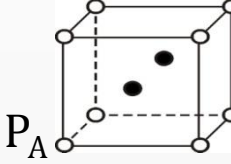
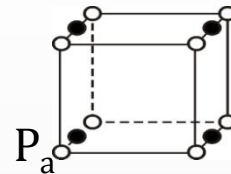
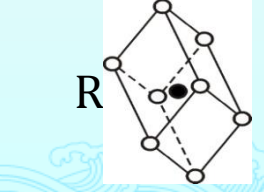
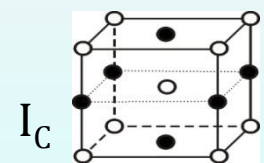
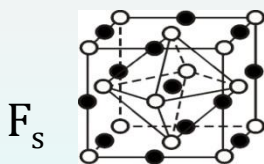
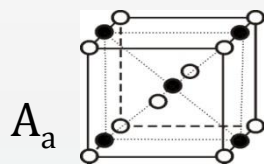
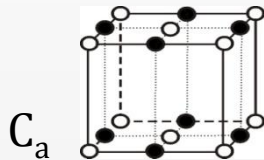
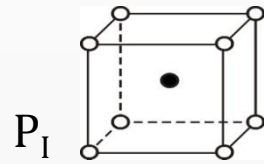
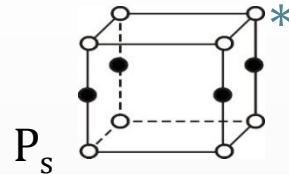
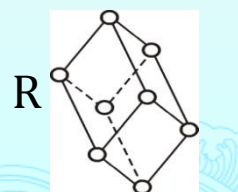
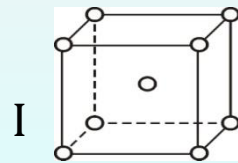
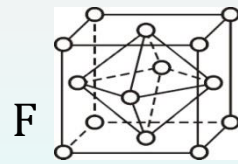
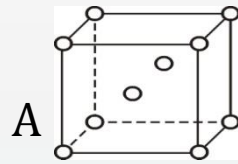
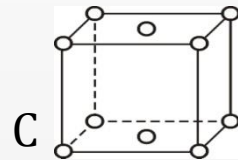
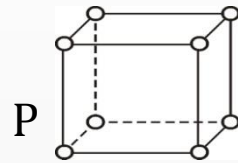


**Data Analysis**  
**GSAS- General Structure Analysis System**

# Magnetic lattice

White

White & Black

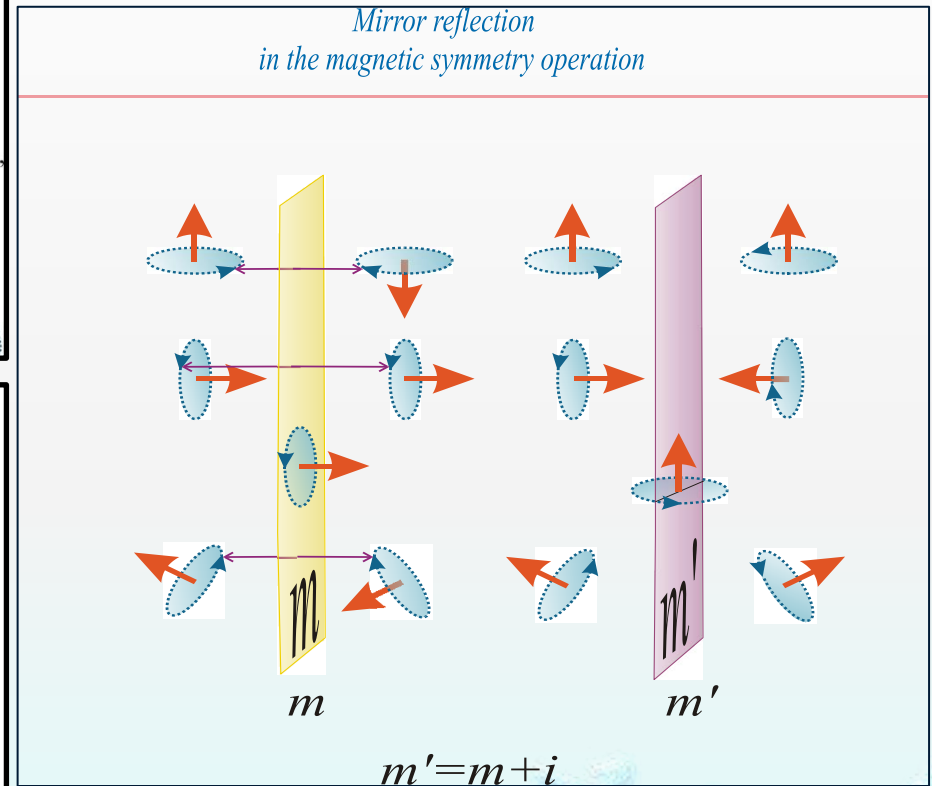
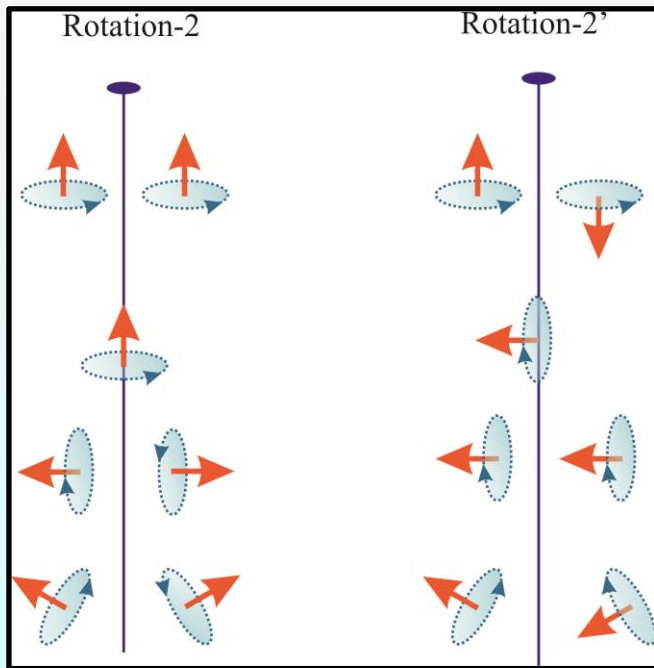
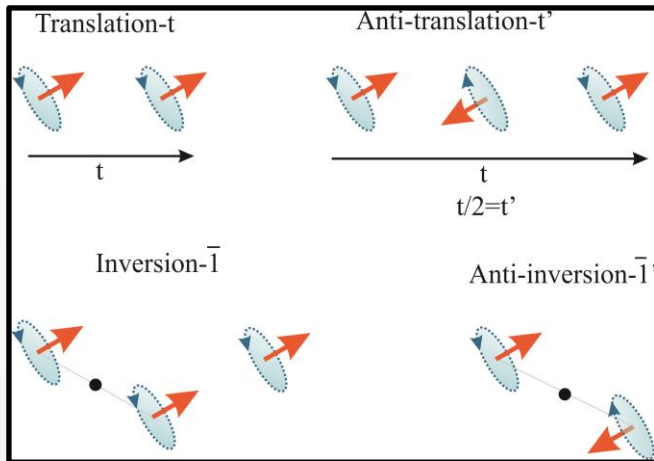


\* Triclinic &  
C<sub>c</sub> in  
Hexagonal  
# Monoclinic

14 (white)  
+ 22 (white&black)  
= 36 magnetic lattice

Ref. N.V.Belov, N.N.Neronora,  
and T.S.Smirnova,  
Soviet Physics,  
Crystallography,  
Vol. 2, #3, 311-322(1957)

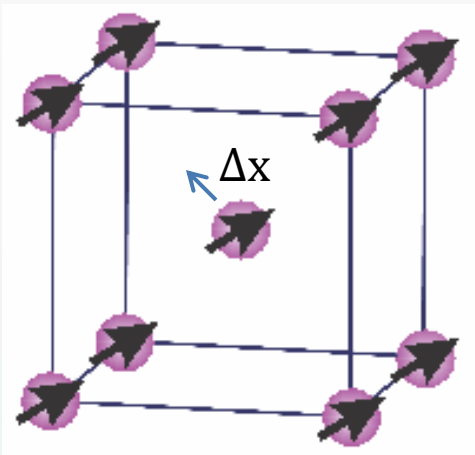
# Some magnetic symmetry operations



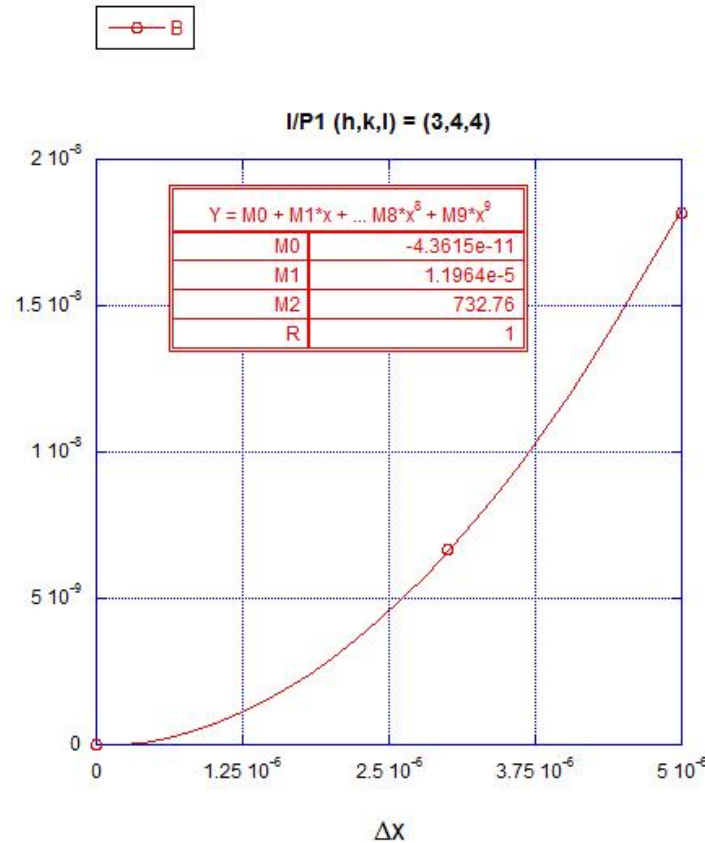


## Reflection condition analysis

$$F_{hkl} = \sum \mathbf{p} \exp(2\pi i(\mathbf{h}x/a_0 + \mathbf{k}y/b_0 + \mathbf{l}z/c_0))$$

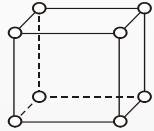
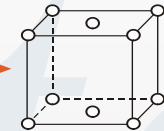
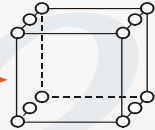
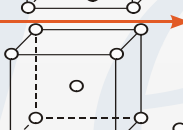
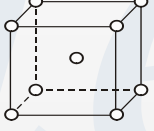

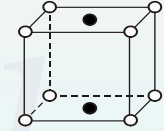
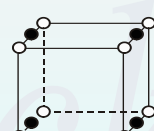
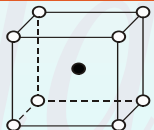



$F^2_{hkl}$



Simulations were done using GSAS. This is the graph of the maximum structure factor as a function of  $\Delta x$ . The threshold of  $10^{-8}$  is passed at approximately  $3.7 \times 10^{-6}$ .

# Integral reflection conditions for centred magnetic (white and black) cells (lattices).

Condition	type	Symbol
<i>None</i>	<i>Primitive</i>	<i>P, R(R)</i> → 
<i><math>-h+k+l=3n</math></i>	<i>Primitive</i>	<i>R(H)</i> → 
<i><math>h+k=2n</math></i>	<i>C-face</i>	<i>C</i> → 
<i><math>k+l=2n</math></i>	<i>A-face</i>	<i>A</i> → 
<i><math>h+k+l=2n</math></i>	<i>Body center</i>	<i>I</i> → 
<i><math>h,k,l</math> all odd or all even</i>	<i>Face center</i>	<i>F</i> → 
<i><math>h+k=2n+1</math></i>	<i>Black C-face</i>	<i>P<sub>C</sub></i> → 
<i><math>h=2n+1</math></i>	<i>Black a-axis</i>	<i>P<sub>a</sub></i> → 
<i><math>h+k+l=2n+1</math></i>	<i>Body center</i>	<i>P<sub>I</sub></i> → 
<i><math>h,k,l</math> all odd</i>	<i>Face center</i>	<i>F<sub>s</sub></i> → 

White: Black; White & Black: Red

## Reflection conditions for symmetry operations

Symmetry Operation	Nuclear Reflection Condition	Magnetic Reflection Condition*
$a$ ( $a$ -glide)	$k + l = 2n$	None
$b$ ( $b$ -glide)	$h + l = 2n$	None
$c$ ( $c$ -glide)	$h + k = 2n$	None
$2_1$	$0k0: k = 2n$	$0k0: k = 2n + 1$
$2'_1$	--	$0k0: k = 2n$

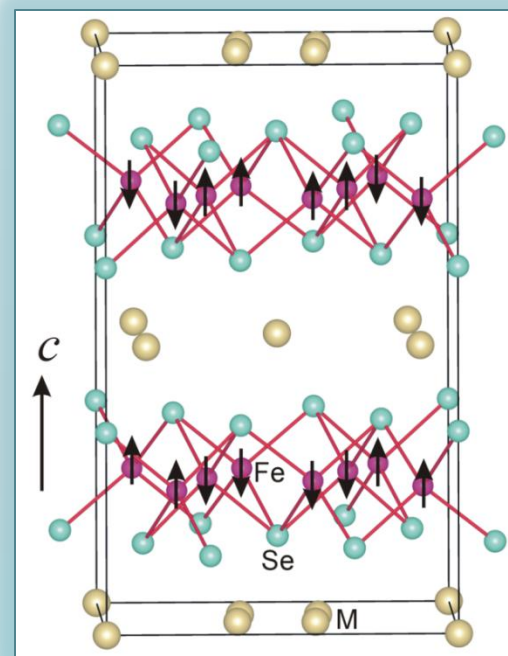
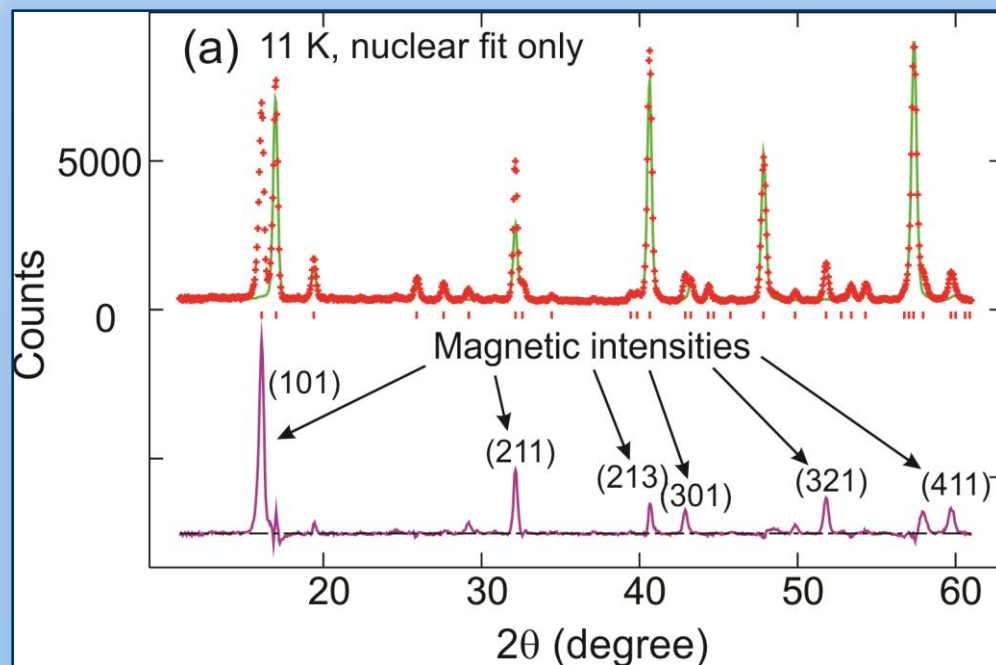
## Reflection conditions for symmetry operations

Symmetry Operation	Nuclear Reflection Condition	Magnetic Reflection Condition*
$4_i$ ( $i=1, 3$ )	$00l: l = 4n$	$00l: l = 2n+1$
$4'_i$ ( $i=1, 3$ )	--	$00l: l = 2n+1$
$3_i$ ( $i = 1, 2$ )	$00l: l = 3n$	$00l: l \neq 3n$
$6_i$ ( $i = 1, 5$ )	$00l: l = 6n$	$00l: l = 2n + 1 \neq 3n$



- ◆ \*For the symmetry operations where the lattice is left ferromagnetic, the magnetic reflection conditions are the same as the nuclear reflection conditions

# Magnetic symmetry for $K_{0.8}Fe_{1.6}Se_2$ : $I4/m'$



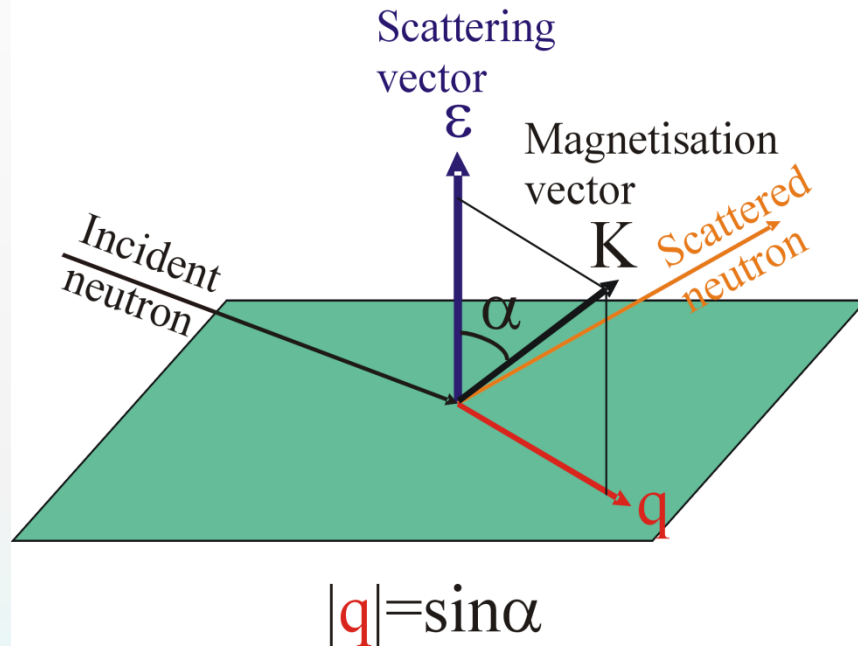
Magnetic reflection condition for  $(h\ k\ l)$ :  $h+k+l=2n$ ,

*Body center lattice*

$I(001)=0$ , Why?

# Magnetic interaction vector

$$\mathbf{q} = \boldsymbol{\varepsilon}(\boldsymbol{\varepsilon} \cdot \mathbf{K}) - \mathbf{K}$$



*Moments //c-axis*  
 $\alpha=0$ , i.e  $\sin \alpha=0$   
 $I(00l)=0$ ,

# Further work

- ◆ Change in magnetic moment amplitude
- ◆ Change in magnetic moment orientation
- ◆ Confirm results by analyzing  $F^2$  formula



# Acknowledgements

Thanks to

- Qing Huang
- Julie Borchers
- Dan Neumann
- Rob Dimeo